

Original article
UDC 656.61.052:004.9
<https://doi.org/10.24143/2073-1574-2025-4-20-25>
EDN SDWZWW

Estimation of the navigation watch system trouble-free operation probability under different time distribution laws restoring the self-monitoring subsystem

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Abstract. With the constant aging of marine vessels, it is becoming increasingly difficult to ensure their navigational safety. Despite the efforts being made, the human factor remains the main cause of accidents in marine and river waters. The necessity of considering the process of keeping a running watch as a system including appropriate subsystems is substantiated. The system of navigation watchkeeping, which includes a subsystem of self-control of the human factor, is being investigated. A model of the information transformation system in ship safety management has been compiled, including a subsystem of self-monitoring. It is noted that the process of information transformation in ship condition management with self-monitoring is capable of ensuring an effective state of safety of the ship, crew and cargo. The assumption is introduced that the recovery time of the subsystem of self-control of the human factor is subject to a degenerate distribution law with a certain mathematical expectation, which will significantly simplify the calculation formulas and create convenient methods for assessing and ensuring reliability (safety) in the navigation watch system. The probability of trouble-free operation of the watchkeeping system is investigated in the case of a degenerate law of the recovery time distribution of the subsystem of self-control of the human factor and in the case when the law of the recovery time distribution is different from the degenerate one. The probability of error-free transformation of information, taking into account self-control, is estimated. The maximum error value in calculating the probability of trouble-free operation of the information conversion system in control is calculated when replacing any law of the distribution of the recovery time of self-control with a degenerate distribution law. An experimental assessment was made of the probability of reliable operation of the navigation watch system under the exponential law of the recovery time distribution of the self-monitoring subsystem.

Keywords: distribution laws, system recovery, navigation watch system, trouble-free operation of the system, reliability of the system, transformations of navigation information

For citation: Iakubovich M. I., Kuznetsova O. B., Penkovskaya K. V., Chirkova Ia. A. Estimation of the navigation watch system trouble-free operation probability under different time distribution laws restoring the self-monitoring subsystem. *Vestnik of Astrakhan State Technical University. Series: Marine engineering and technologies.* 2025;4:20-25. (In Russ.). <https://doi.org/10.24143/2073-1574-2025-4-20-25>. EDN SDWZWW.

Научная статья

Оценка вероятности безаварийной работы системы несения ходовой вахты при различных законах распределения времени восстановления подсистемы самоконтроля

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Аннотация. В условиях постоянного старения морских судов все сложнее становится обеспечивать их навигационную безопасность. Несмотря на предпринимаемые усилия, человеческий фактор остается основной причиной аварий в морских и речных акваториях. Обоснована необходимость рассмотрения процесса несения ходовой вахты как системы, включающей соответствующие подсистемы. Исследуется система несения ходовой вахты, включающая подсистему самоконтроля человеческого фактора. Составлена модель системы преобразования информации в управлении состоянием безопасности судна, включающая подсистему самоконтроля. Отмечено, что процесс преобразования информации в управлении состоянием судна с самоконтролем способен обеспечить эффективное состояние безопасности судна, экипажа и груза. Введено допущение о том, что время восстановления подсистемы самоконтроля человеческого фактора подчиняется вырожденному закону распределения с определенным математическим ожиданием, что позволит существенно упростить расчетные формулы и создать удобные методики для оценки и обеспечения надежности (безаварийности) в системе несения ходовой вахты. Исследована вероятность безаварийной работы системы несения вахты при вырожденном законе распределения времени восстановления подсистемы самоконтроля человеческого фактора и в случае, когда закон распределения времени восстановления отличается от вырожденного. Проведена оценка вероятности безошибочного преобразования информации с учетом самоконтроля. Рассчитана предельная величина погрешности в вычислении вероятности безаварийной работы системы преобразования информации в управлении при замене любого закона распределения времени восстановления самоконтроля на вырожденный закон распределения. Произведена экспериментальная оценка вероятности надежной работы системы несения ходовой вахты при экспоненциальном законе распределения времени восстановления подсистемы самоконтроля.

Ключевые слова: законы распределения, восстановление системы, система несения ходовой вахты, безаварийная работа системы, надежность работы системы, преобразования навигационной информации

Для цитирования: Якубович М. И., Кузнецова О. Б., Пеньковская К. В., Чиркова Я. А. Оценка вероятности безаварийной работы системы несения ходовой вахты при различных законах распределения времени восстановления подсистемы самоконтроля // Вестник Астраханского государственного технического университета. Серия: Морская техника и технология. 2025. № 4. С. 20–25. <https://doi.org/10.24143/2073-1574-2025-4-20-25>. EDN SDWZWW.

Introduction

According to expert estimates, the bulk of Russia's civilian fleet consists of heavily depreciated vessels – the average age of vessels exceeds 38 years – requiring special attention to the navigational safety of these vessels. An annual analysis of accidents involving maritime and river transport shows that accidents involving older vessels lead to human casualties and serious environmental consequences. Therefore, it is essential to prioritize ensuring navigational safety and minimizing accidents.

Research shows a disturbing trend: human error often leads to accidents. Fatigue is a particularly pressing issue among seafarers. The most recent widely discussed incident involved a second officer falling asleep on watch, leading to a vessel running aground in Norway, narrowly missing a residential building. In the Russian segment, in July, a tugboat collided with the hull of a cargo ship in the waters of the Nakhodka commercial port. The key cause of the navigational accident was the tugboat captain's fatigue, who fell asleep and lost control of the vessel.

The human factor, coupled with an aging vessel, can lead to serious consequences for vessel safety, confirming the need for further research into the navigational watchkeeping process, considering it as a system with corresponding subsystems. This approach will allow for more comprehensive use of mathematical distribution laws to ensure accident-free naviga-

tional watchkeeping.

Thus, the navigational watchkeeping system includes a “human factor” self-monitoring subsystem, i.e., a process of vessel state management with self-monitoring of the conversion of navigational information into control, ensuring the safety of the vessel, crew, and cargo. The self-monitoring subsystem should only be activated in the event of an emergency, so hidden failures are possible during prolonged self-monitoring.

In order to identify hidden failures in the operation of the self-monitoring subsystem with the aim of increasing the reliability of the navigation watch, over time τ at equal time intervals τ_0 the decision maker must conduct m sessions of checking the operability and restoration of the self-monitoring subsystem with a duration τ_B .

During time τ_B the system for converting navigational information into ship control functions without the use of the self-monitoring subsystem. However, an emergency can occur either during the interval τ_0 , when the self-monitoring subsystem fails and only then will an emergency occur, or when an emergency occurs, with the subsystem being restored again during time τ_B .

Further, we will assume that the recovery time of the human factors self-monitoring subsystem obeys a degenerate distribution law with a mathematical expectation $M[\tau_B] = C [1, 2]$. This assumption allows us to significantly simplify calculation formulas and create convenient methods for assessing and ensuring the trouble-free operation of the watchkeeping system.

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In practice, the recovery time of the self-monitoring subsystem is a random variable that cannot be considered constant [3]. In this regard, it is important to analyze the influence of the distribution of the subsystem recovery time on the probability of trouble-free operation of the watchkeeping system, taking into account the operation of the self-monitoring subsystem. For this purpose, we will compare the probability of trouble-free operation of the watchkeeping system under a degenerate distribution law of the subsystem recovery time with the probability of trouble-free operation of the watchkeeping system under other laws, but with the same mathematical expectation of the subsystem recovery time.

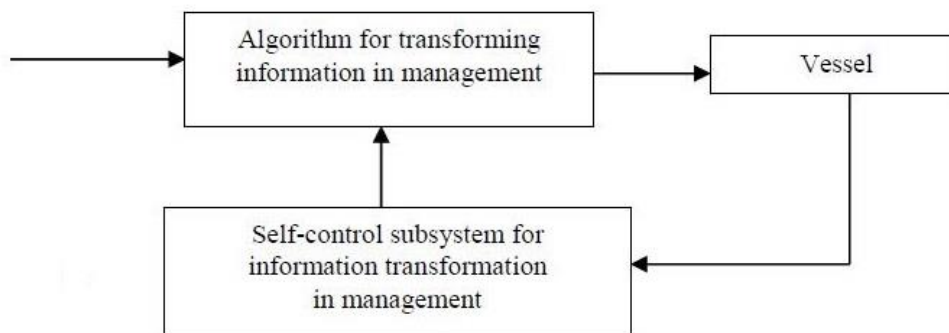


Fig. 1. An algorithm for converting navigation information into ship condition management with a self-monitoring subsystem

Then, in the system (Fig. 1), the probability of failure-free operation of the watchkeeping system with the self-monitoring subsystem over the time interval from τ_1 to τ_2 , where the times τ_1 and τ_2 are counted from the

start of the watchkeeping, with a degenerate distribution law of the subsystem recovery time, is denoted by $P[\tau_1, \tau_2]$.

The following expressions are valid for this probability:

$$\begin{aligned} P[0, m\tau_0] &= P[0, \tau_0] \{P[\tau_0, 2\tau_0]\}^{m-1}; \\ P[0, \tau_0] &= 1 - \int_0^{\tau_0} F(\tau_0 - t) dF_H(t); \\ P[\tau_0, 2\tau_0] &= [1 - F(\tau_B)] \left[1 - \int_0^{\tau_0 - \tau_B} F(\tau_0 - \tau_B - t) dF_B(t) \right]. \end{aligned} \quad (1)$$

The probability $P[\tau_0, 2\tau_0]$ is a function of $\tau_B = C$, the recovery time of the self-monitoring subsystem. For convenience, when studying the dependence of $P[\tau_0, 2\tau_0]$ on $M[\tau_B]$, $P[\tau_0, 2\tau_0]$ will be denoted by $P(M[\tau_B])$ or simply $P(\tau_B)$. In the case where the distribution law of the protection recovery time $F_B(t)$ is non-degenerate, the probability of an accident-free watch with self-monitoring for the time from τ_1 to τ_2 , where the times τ_1 and τ_2 are counted from the start of the watch, is denoted by $P[\tau_1, \tau_2]$.

For this probability, the following formulas are valid:

$$\begin{aligned} P^*[0, m\tau_0] &= P[0, \tau_0] \{P^*[\tau_0, 2\tau_0]\}^{m-1}; \\ P^*[\tau_0, 2\tau_0] &= \int_0^{\tau_0} P(\tau_B) dF_B(\tau_B / \tau_B < \tau_0). \end{aligned} \quad (2)$$

The probability $P^*[\tau_0, 2\tau_0]$ is a function of the mathematical expectation $M[\tau_B]$ of the verification time of the process of converting navigation information into controls. We denote this function by $P^*(M[\tau_B])$. In particular, for some specific distribution laws of the failure-free operation time of the self-monitoring subsystem (Fig. 1) and the recovery time of this subsystem, expressions (1) and (2) can be represented as specific, but rather complex dependencies. At the same time, if we denote the function $P[0, m\tau_0]$ by P_m and the function of the form $P^*[0, m\tau_0]$ by P_m^* , then we can assert that the function $P[0, m\tau_0]$ is decreasing with respect to $M[\tau_B]$.

Further, it can be shown that for any distribution law $F_B(t)$ the relative positions of the functions

$P[0, m\tau_0]$ and $P^*[0, m\tau_0]$ with respect to $M[\tau_B]$ can be determined. For this purpose, it is sufficient to use Jensen's integral formula [4], according to which the following inequality is valid:

$$P\left(\int_0^{\tau_0} f_B(\tau_B / \tau_B < \tau_0) \tau_B d\tau_B / \int_0^{\tau_0} f_B(\tau_B / \tau_B < \tau_0) d\tau_B\right) \leq \int_0^{\tau_0} P(\tau_B) P f_B(\tau_B / \tau_B < \tau_0) d\tau_B / \int_0^{\tau_0} f_B(\tau_B / \tau_B < \tau_0) d\tau_B.$$

If the function $P(\tau_B)$ is convex, then the sign in this inequality is preserved, and if the function $P(\tau_B)$ is concave, then the sign in this inequality is reversed. Accordingly, depending on whether the function $P(\tau_B)$ is convex or concave, the graphs of P_m^* lie either not below or not above the graph P_m .

Analysis of the function $P(\tau_B)$ for convexity and mutual arrangement

When examining the convexity of the function $P(\tau_B)$, it is known that the function is convex if its first derivative is increasing, and concave if its first derivative is decreasing.

Having considered various distribution laws, we can conclude that, for any distribution law $F_B(t)$, the relative positions of the graphs of the functions $P[0, m\tau_0]$ and $P^*[0, m\tau_0]$ are as follows:

1) if $F_H(t) = 1 - e^{-\lambda_H t}$ is an exponential distribution, then for $\lambda > \lambda_H$ the P_m^* graphs are not located below the P_m graph, for $\lambda = \lambda_H$ the P_m^* graphs and the P_m graph coincide, and for $\lambda < \lambda_H$ the P_m^* graphs are not located above the P_m graph;

2) if $F_H(t) = 1 - (2t / T_H) e^{-2t/T_H} - e^{-2t/T_H}$ is the first order Erlang distribution, then the P_m^* graphs are located not lower than the P_m graph when

$$2/T_H - \lambda \leq 0, \quad 2/T_{H_2} - \lambda > 0$$

$$\text{and } \tau_0 \leq \lambda / (2/T_H)(2/T_H - \lambda);$$

3) if $F_H(t) = 1 - e^{-\beta t}$, $\alpha, \beta > 0$ is the Weibull distribution, then the P_m^* graphs are located not lower

than the P_m graph when

$$\tau_0 \leq (1/\alpha\beta)^{1/(\alpha-1)};$$

4) if $F_H'(t) = t e^{-t/\beta} / \beta^{\alpha+1} G(\alpha+1)$, $\beta > 0$ (α is an integer) is a gamma distribution, then the P_m^* graphs are located not lower than the P_m graph when $\lambda \leq 1/\beta$.

For the second and third cases, with parameter relationships not considered above, the function $P(\tau_B)$ is neither convex nor concave. With such parameter relationships, the graphs of P_m^* and P_m may intersect.

In the fourth case, the inequality $\lambda \geq 1/\beta$ is only a sufficient condition for the convexity of the function $P(\tau_B)$. For $\lambda < 1/\beta$, the analytical expressions obtained when examining the convexity of the function $P(\tau_B)$ are so cumbersome that their practical use is impossible.

It should be noted here that the Rayleigh distribution law can be considered as a special case of the Weibull distribution law for $\alpha = 2$, and $\beta = 1/2\sigma^2$ [5, 6]. Consequently, the considered basic distribution laws, for which the study of the function $P(\tau_B)$ for convexity yields fairly simple analytical expressions. In other cases (as, for example, for the normal distribution law), the study can only be carried out by a numerical method.

Estimation of the probability of error-free transformation of information taking into account self-monitoring

The conducted analysis of the convexity conditions of the $P(\tau_B)$ function allows us to formulate a methodology for assessing the probability of reliable operation of the navigation information conversion system in managing the state of ship navigation safety under any distribution law of the self-monitoring subsystem recovery time.

The probability of error-free operation of the information conversion system in control with the self-monitoring subsystem over time $m\tau_0$ can be found using the approximate expression

$$P_{tr}[0, m\tau_0] = P[0, \tau_0] \{P_{tr}[\tau_0, 2\tau_0]\}^{m-1},$$

where

$$P_{tr}[\tau_0, 2\tau_0] = 1 - \int_0^{\tau_0} F(\tau_0 - t) dF_H(t) - \lambda e^{-\lambda M[\tau_0]} (1 - F_H(\tau_0 - M[\tau_B])) M[\tau_B]$$

with an error Δ , not exceeding the value:

– for a degenerate distribution law

$$|\Delta_1| < [(P_{tr}[\tau_0, 2\tau_0] + \delta_1)^{m-1} - P_{tr}^{m-1}[\tau_0, 2\tau_0]] P[0, \tau_0] \approx (m-1) \delta_2 P_{tr}^{m-2}[\tau_0, 2\tau_0] P[0, \tau_0];$$

– for any other distribution law

$$|\Delta_2| < [(P_{tr}[\tau_0, 2\tau_0] + \delta_2)^{m-1} - P_{tr}^{m-1}[\tau_0, 2\tau_0]] P[0, \tau_0] \approx (m-1) \delta_2 P_{tr}^{m-2}[\tau_0, 2\tau_0] P[0, \tau_0],$$

where

$$\delta_1 = M[\tau_B] \max\{\lambda(1 - F_H(\tau_0))(1 - e^{-\lambda M[\tau_0]}), \lambda[F_H(\tau_0) - F_H(\tau_0) - M[\tau_B]]\};$$

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$$\delta_2 = M[\tau_B] \max\{\lambda(1 - F_H(\tau_0))(1 - e^{-\lambda T_B}), \lambda[F_H(\tau_0) - F_H(\tau_0 - T_B)]\} + \\ + \int_0^{\tau_0} \tau_B f_B(\tau_B / \tau_0 < \tau_0) d\tau_B \max\{\lambda(1 - F_H(\tau_0))(1 - e^{-\lambda \tau_0}), \lambda(1 - F_H(\tau_0))\}.$$

In this case, the error Δ_3 in calculating the probability of trouble-free operation of the information conversion system in control over time $m\tau_0$ when replacing

any distribution law of the self-control recovery time τ_B with a degenerate distribution law will not exceed the value

$$|\Delta_3| \leq [(P_{ir}[\tau_0, 2\tau_0] + \delta_1 + \delta_2)^{m-1} - P_{ir}^{m-1}[t_0, 2\tau_0]] P[0, \tau_0] \approx \\ \approx (m-1)(\delta_1 + \delta_2) P_{ir}^{m-2}[\tau_0, 2\tau_0] P[0, \tau_0].$$

Experimental assessment of the reliability of the navigational watchkeeping system

We will conduct an experimental assessment of the probability of reliable operation of the navigation information conversion system in managing the ship's navigational safety status with an exponential distribution of the self-monitoring subsystem recovery time. The initial data was analyzed over 100 hours

of watchkeeping, which included twenty-five watches, with hidden failures of the self-monitoring subsystem occurring during eight watches. To construct a statistical series, the total watchkeeping time (100 hours) was divided into ten intervals (categories) of 10 hours each for each categorization. A histogram of the probability of failure of the self-monitoring subsystem of the watchkeeping system is shown in Fig. 2.

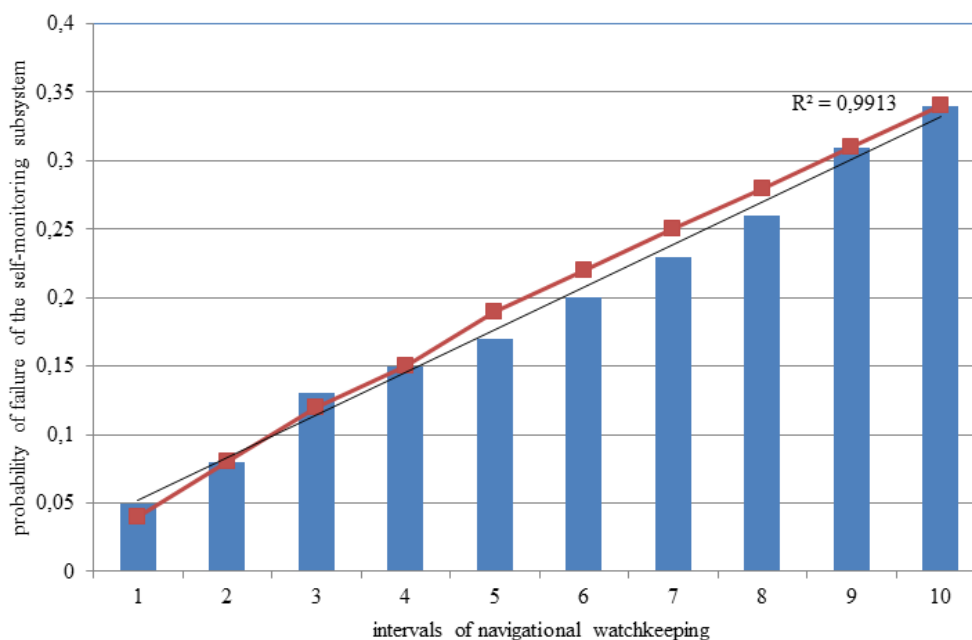


Fig. 2. Histogram of the probability of failure of the self-monitoring subsystem of the navigation watch system

The calculated coefficient of determination (0.99) indicates a very high degree of data conformity with the model, i.e., the model explains their variation almost perfectly. Thus, the exponential distribution model of the self-monitoring subsystem's recovery time can be used for an a priori analysis of the reliability of watchkeeping, which is important for voyage planning and ensuring navigational safety.

Conclusion

For information conversion systems in control, the

probability of error-free operation of this system with a degenerate self-monitoring recovery time distribution law is the lower or upper limit of the probability of error-free operation of the entire system with any other self-monitoring recovery time distribution law. The error in calculating the probability of error-free operation of a conversion system with self-monitoring when replacing an exact formula with an approximate one, or any self-monitoring recovery time distribution law with a degenerate law, is insignificant and can practically be ignored altogether. When developing methods

for assessing and ensuring the reliability of information conversion systems, taking into account the use of self-monitoring subsystems, it is practically possible to use

any self-monitoring recovery time distribution that allows for simplifying the calculation formulas.

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The article was submitted 15.04.2025; approved after reviewing 16.09.2025; accepted for publication 05.11.2025
Статья поступила в редакцию 15.04.2025; одобрена после рецензирования 16.09.2025; принята к публикации 05.11.2025

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